



FIRST
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Computer Science Department
Comp232 First Hour Exam
Fall 1999

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Iyad Jaber

- This question paper is composed of five pages containing four questions.
- Please read the whole paper before starting to answer.
- You have ten minutes to read the paper and then only twenty minutes to ask questions.
- The only questions allowed concern the spelling and the meaning of English words.
- Intermediate reasoning steps are demanded. Any unjustified answer is not accepted.
- Remember to write down you're your full name and your student id number.

Question1(25%)

Ordered lists are special lists that keep their elements sorted in an increasing order. An ordered list supports basically the following operations:

1. **Insert:**
Inserts an element in the list at the right position so as to keep the list sorted in an increasing order.
2. **Delete:**
Deletes a node from the list.

The structures and types to be used are given by the file OList.h:

```

/* Type declaration for linked list implementation of the OList.h */
#define FAILURE (0)
#define SUCCESS (1)

```

```

struct Node;
typedef struct Node *PtrNode;
typedef struct PtrNode OList;

```

```

struct Node {
    int Element;
    PtrNode Next;
}

```

Using linked list (with dummy header) implementation and the declarations given by OList.h, complete the two basic operations, Insert and Delete.

```

/* deletes the node pointed by the variable node from list*/
int Delete (OList list, PtrNode node)
{ PtrNode p; if (list == NULL || node == NULL)
  p = FindPrevious (node, list);
  if (p->Next == NULL)
  { cout << "Node wasn't found";
    return FAILURE;
  }
  p->Next = node->Next;
  free (node);
  return SUCCESS;
}

```

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link failure

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/* Inserts a new element in the list
while respecting the increasing order */

int insert (OList list, int value)

{
PtrNode p; if (list == NULL) return Failure;

p = list;

while (p->Next != NULL && p->Next->Element < value)

p = p->Next ✓

PtrNode temp;

temp = (PtrNode) malloc (sizeof (struct Node));

if (temp == NULL)

return FAILURE; ✓

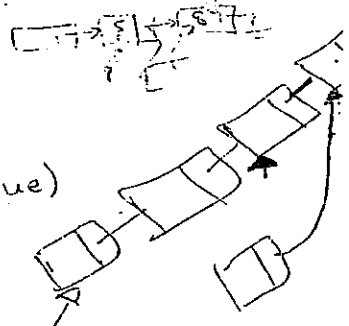
temp->Next = p->Next; ✓

p->Next = temp; ✓

temp->Element = value; ✓

return SUCCESS; ✓

}



PtrNode FindNode (PtrNode node, OList list)

{ PtrNode p;

p = list;

while (p->Next != NULL && p->Next->Element != node)

p = p->Next; ✓

return p;

$$n = \# \text{ of data} = \text{high} - \text{low} + 1$$

$$T(n) = \begin{cases} d, & n=1 \\ c + T\left(\frac{n}{2}\right), & n > 1 \end{cases}$$

since the function divides the array in each move, into half

$$T\left(\frac{n}{2}\right) = c + T\left(\frac{n}{4}\right)$$

$$T(n) = 2c + T\left(\frac{n}{4}\right)$$

$$= ic + T\left(\frac{n}{2^i}\right)$$

$$T(n) = \begin{cases} d, & n=1 \\ T\left(\frac{n}{2}\right), & n > 1 \end{cases}$$

$$\frac{n}{2^i} = 1 \Rightarrow i = \log_2 n$$

$$T\left(\frac{n}{2}\right) = T\left(\frac{n}{4}\right)$$

$$T(n) = T\left(\frac{n}{2^i}\right)$$

$$\frac{n}{2^i} = 1$$

$$n = 2^i$$

$$i = \log_2 n$$

$$T(n_1, n_2) = \begin{cases} T\left(\frac{n_1+n_2}{2}, \frac{n_1+n_2}{2}\right) \\ T\left(n_1, \frac{n_1+n_2}{2}-1\right) \end{cases}$$

$$T\left(\frac{n_1+n_2}{2}, n_2\right) = T\left(\frac{n_1+2n_2}{2}, n_2\right)$$

$$= T\left(\frac{n_1+3n_2}{2}, n_2\right)$$

$$\frac{n_1+3n_2}{2} = 1$$

$$i = \frac{2-n_1}{n_2}$$

$$n_1 + 1n_2 = 2$$

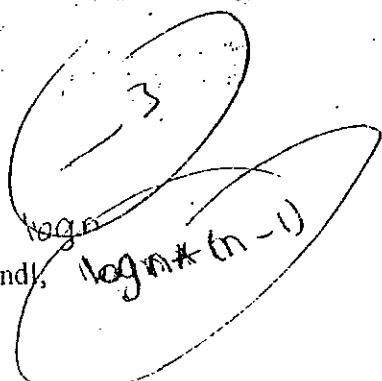
Question 2 (25%)

What is the worst case running time a function of n of the following code fragments

```

a)
for(j = 0; j < n; j++)
    for(s = 0; s < n^2; s++)
        for(k = j; k < j * j; k++)
        {
            t = j;
            while (t > 0)
            {
                for(d = 0; d < t; d++)
                    cout << d << endl;
                t /= 2;
            }
        }
    
```

? $n + \frac{n}{2} + \frac{n}{4} + \frac{n}{8} \dots < 2n$



$$T(n) = n * n^2 * (n^2 - n) * \log n * (n - 1)$$

$$= O(n^6 \log n) = O(n^6 \log n)$$

```

b)
int B_S ( int a[], int low, int high, int x)
{
    C1 int mid;
    C2 if ( low < high)
    {
        C3 mid = ( low + high ) / 2;
        C4 if ( a[mid] == x)
        C5 return mid;
        C6 else
        C7 if ( a[mid] < x)
        C8 B_S ( a, mid+1, high, x);
        C9 else
        C10 B_S ( a, low, mid-1, x);
    }
    C11 else
    C12 return -1;
}
    
```

since each traverse of the function divides the array into two
 assume $n = \#$ of data elements = high - low + 1

$$T(n) = \begin{cases} d, & n = 1 \\ T(\frac{n}{2}) + c, & n > 1 \end{cases}$$

$$T(n) = ic + T(\frac{n}{2^i})$$

base case $\frac{n}{2^i} = 1$
 $2^i = n \Rightarrow i = \log n$

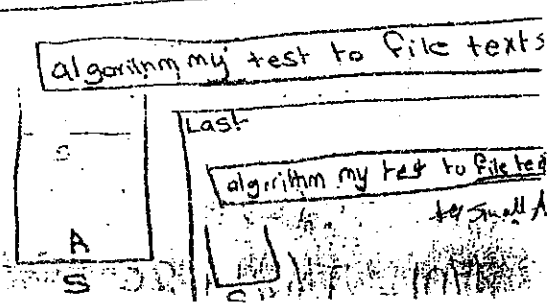
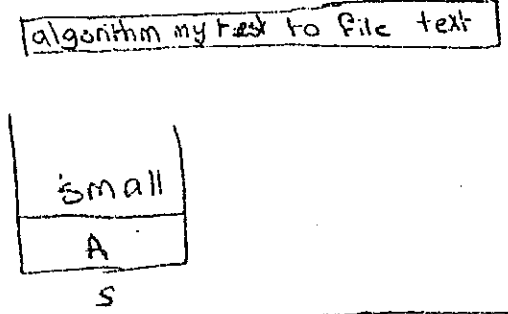
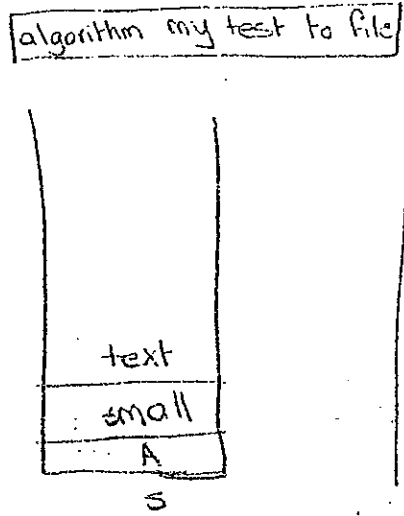
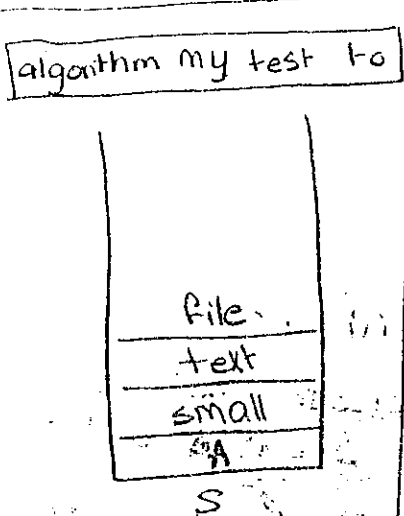
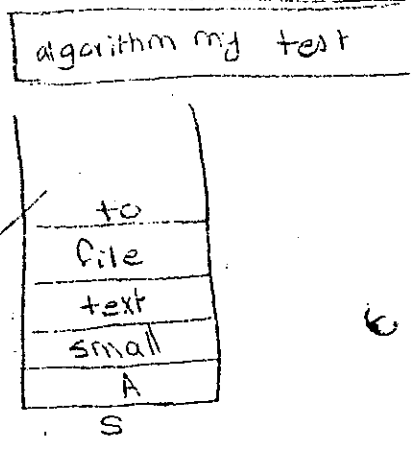
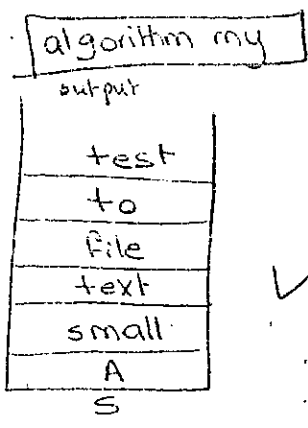
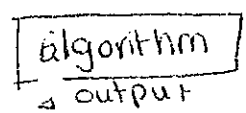
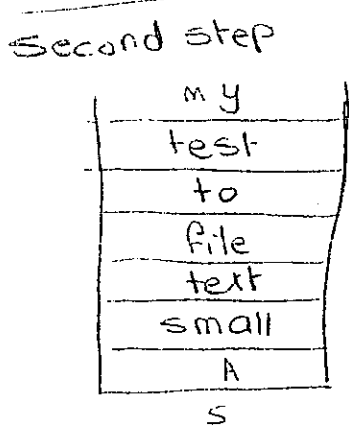
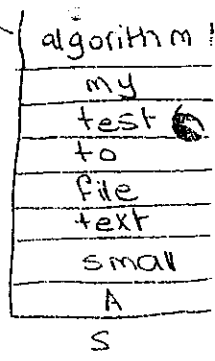
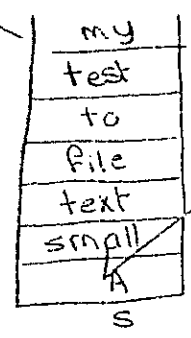
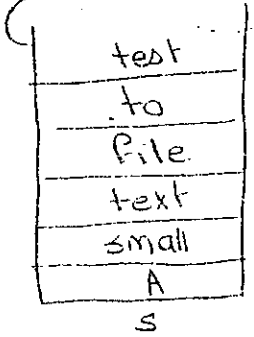
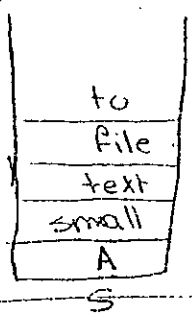
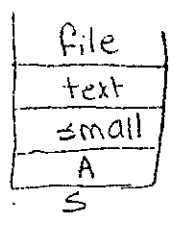
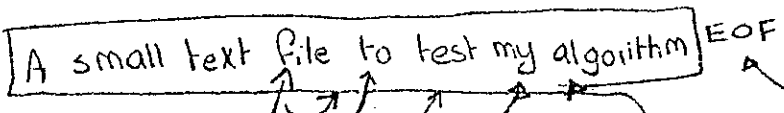
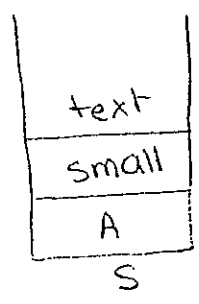
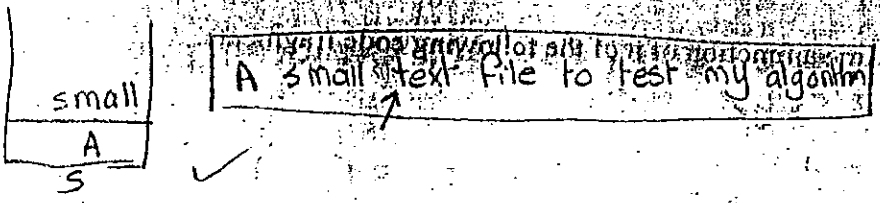
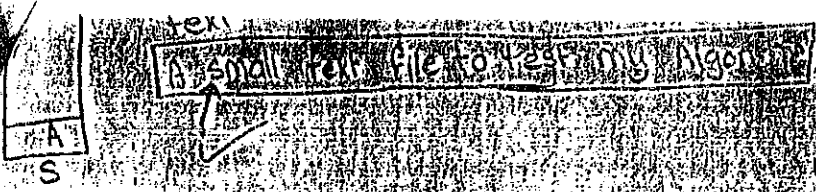
$$T(\frac{n}{2}) = T(\frac{n}{4}) + c$$

$$T(n) = c \cdot \log n + T(1)$$

$$= c \cdot \log n + d$$

$$\Rightarrow O(\log n)$$

$$T(n) = T(\frac{n}{4}) + 2c$$



Question 3 (25%)

Write a pseudo-code function to read a sequential text file. Each line in the file contains a number of words. All words terminate with a white-space (' '). Print the words contained in the file in the reverse order in which you read them.

Suppose that you are provided with a function that returns the current word from the file and advances the file pointer to the next word. If EOF is reached, this function returns NULL.

```
char * ReadWord ()
```

1. You should very clearly describe the data structure that will be used to solve this problem and how the data structure should be applied (give the names of the basic operations supported by your data structure).
2. Apply the algorithm described in 1 on the following text file. Show clearly all the intermediate steps using figures to represent the consecutive states of your data structure.

A small text file to test my algorithm

Demo Text File

1. Data Structure is Stack, with Link List Implementation
Elementary Operations: used Stack because LIFO
 1) push 2) pop ~~3) create~~ 3) Top 4) is-empty

```
void Print_reverse (ifstream text, Stack S)
{
    char * String = ReadWord()
    while (String != NULL)
    {
        Push (S, String);
        String = ReadWord();
    }
    while (! is-empty (S))
    {
        cout << Top (S) << ' ';
        Pop (S);
    }
    cout << endl;
    text.close();
}

```

```
struct node
{
    element-type element;
    nodeptr next;
}

void push (Stack S, element-type
char *
)
{
    nodeptr p;
    p = (nodeptr) malloc (sizeof (struct
    if (p == NULL)
    {
        cout << "Error"
        exit (1);
    }
    p->element = x;
    p->next = S->next;
    S->next = p;
}

```

Elementary Stack Operations:

* Definition of Stack,

```
typedef struct node * nodeptr;
```

```
typedef nodeptr Stack;
```

```
typedef char * element-type;
```

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24

```

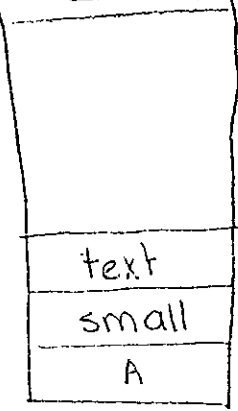
depth(p)
p->S->next
S->next = p->next
free(p)
}

return (S->next == NULL) ?
element_type Top(stack S)
return S->next->element
}

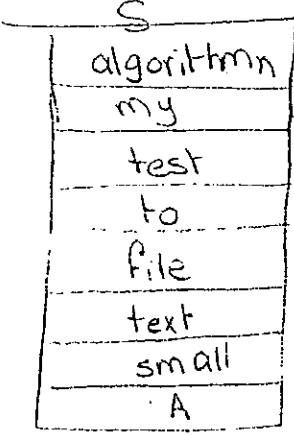
```



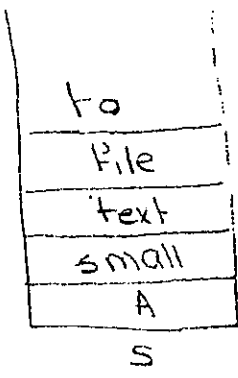
A small text file to test my algorithm



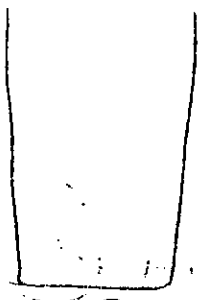
/* after three words are pushed into the stack */



/* after all the file is read into the stack */



algorithm my test
output



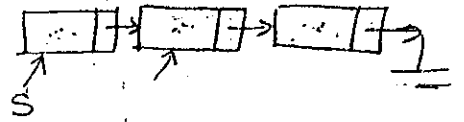
algorithm my test to file text small A

See at the back of previous page.

Question 4 (25%)

Write a recursive function, `rec_display`, to display the items in a stack on a single output line, with the bottom element printed first, and the top element printed last. For efficiency, pass the stack by reference, but make sure the stack has been restored to its original state when the function terminates.

```
void rec_display (Stack S)
{
    if (S->next != NULL)
        rec_display (S->next);
    cout << S->element << " ";
}
```



/ Note: this function receives the node next to the header not the header itself*

```
so in main ()
{
    Stack S;
    rec_display (S->next);
    cout << endl;
}
```

**/*

→ */* necessary declarations */*

```
typedef struct node * nodeptr;
struct node
{
    element_type element;
    nodeptr next;
}
typedef nodeptr Stack;
```


Math. and Computer Department
Computer 232
First Hour Exam (Winter 1998)

70
100

Instructor: Nael Qaraeen

Student Name: _____

Student id#: _____

(20%)

Q1) Give an analysis of the running time in terms of N for the following code fragments (Use *Big-Oh* notation)

a.

```
sum = 0;
for ( I=0; I < N; I++)  $N$ 
  for (j=0; j < I * I; j++)  $N^2$ 
    for (k=0; k < j; k++)  $N^2$ 
      sum++;
```

Order of magnitude = $O(N^3)$

b.

```
int B_S(const Elementtype a[], Elementtype X, int N)
{
  int low, mid, high;
  low = 0; high = N - 1;
  while (low <= high)
  {
    mid = (low + high) / 2;
    if (a[mid] < X)
      low = mid + 1;
    else
      if (a[mid] > X)
        high = mid - 1;
    else
      return mid;
  }
  return -1;
}
```

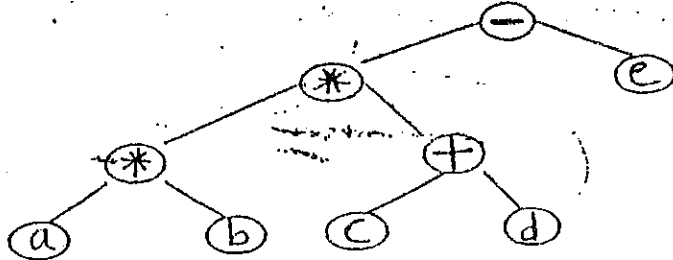
Order of magnitude = ~~$O(N)$~~ $O(\log N)$

7

(30%)

Q2)

a. Give the Infix and Postfix expressions corresponding to the tree below:



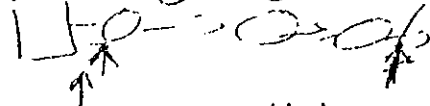
(I) Infix expression = $a * b * (c + d) - e$

(II) Postfix expression = $ab * cd + * e -$

b. Describe how you would insert an element at the bottom of a stack without affecting the order of the other elements already in the stack

~~and we can do that because the order of the stack is affected and we can do it by putting all elements in the stack and all put the insert the new element at the bottom and after the insertion the stack~~
we can do that by letting the stack to shift to an array so we can shift the element and put the new one in the bottom of the stack

linked list



c. Suppose you have a queue ADT implemented as an array stored in k memory cells. When will this queue be empty in terms of the *Front* and *Rear* of the queue?

it will be empty when $rear = front - 1$

2.5

(20%)

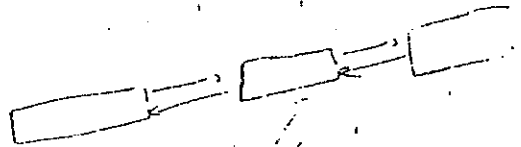
Q3) Given a *doubly linked list* of nodes. Using the following definitions, fill in the body of the insert function below which allows you to insert a node with element *X* after the node at position *P* in the doubly linked list *L*.

Struct Node;

```
typedef struct Node *PtrToNode;  
typedef struct PtrToNode List;  
typedef struct PtrToNode Position;
```

Struct Node

```
{  
    ElementType element;  
    Position prev;  
    Position next;  
}
```



Position insert(ElementType X, List L, Position P)

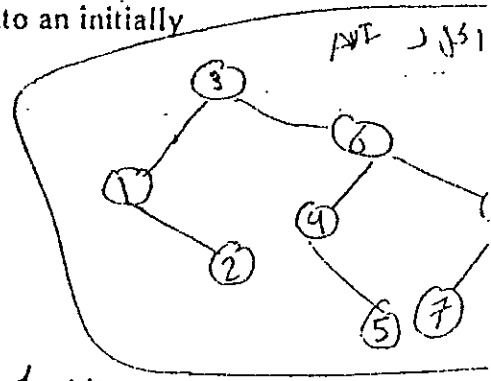
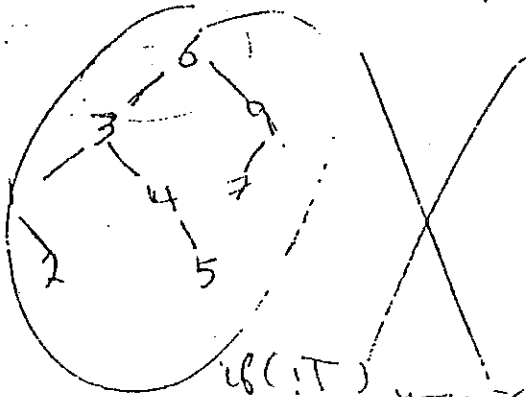
```
{  
    Position tmp, cell;  
    tmp = malloc(sizeof struct node);  
    if (tmp == null)  
        cout << "error out of space";  
    else  
    {  
        cell = P->next;  
        tmp->element = X;  
        tmp->next = cell;  
        P->next = tmp;  
        tmp->prev = P;  
        cell->prev = tmp;  
    }  
    return P; -1  
}
```

what if p->next;
-4

) /* End of function insert */

(30%)
Q4)

a. Show the result of inserting the following numbers in order into an initially empty binary search tree:
3, 1, 4, 6, 9, 2, 5, 7



if (!T) ...
if (T < T) ...
T -> left = del (...)

b. Is the tree generated in (a) above considered an AVL tree? Why? NO

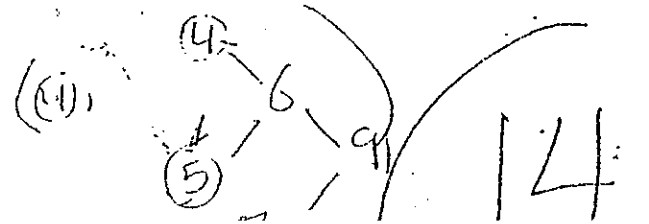
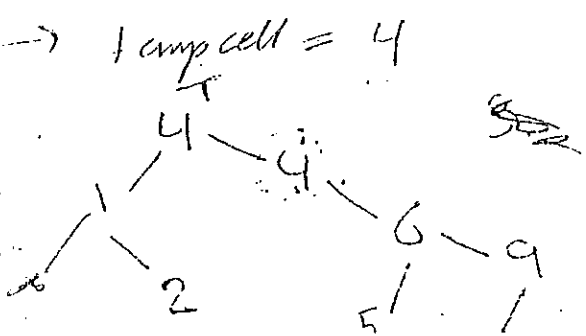
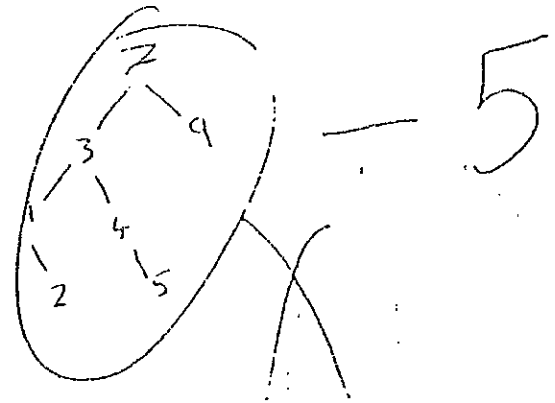
~~Yes~~ Yes

نعم نعم، وذلك لأنه لا يشترط أن تكون AVL tree. Binary tree وان يكون
الترتيب حسب القيمة وليس فقط edge داخله وان يكون Balance

because the ^{edges} left side and right side of each node must be such that $(left - right) < 2$... one just

c. Show the result of deleting the root of the binary search tree in (a) above.

here
For each ~~tree~~ node in tree the height of left and right subtree must differ by at most 1



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Computer Science Dept
Comp. 232
First Hour Exam

Instructor: Iyad Jaber

Date: 31/03/2000

Question #1 (25%)

Suppose we have an array based list $A[0..n-1]$ and we want to delete all duplicates. Last position is initially $n-1$, but gets smaller as elements are deleted. Consider the pseudo code program fragment in figure bellow. The procedure DELETE deletes the element in position J and collapses the list.

- Explain how this procedure works.
- Rewrite this procedure using general list operations.
- Using a standard array implementation, what is the running time of this procedure?
- What is the running time using a linked list implementation?

```

for (int I=0; I< Last_Position; I++)
{
  int J= I+1;
  while (J < last_Position)

```

```

    if (A[I] == A[J]);
        Remove(J);
    else
        J++;

```

Time

$$\begin{aligned}
& n(1 + (n-1)(1)) \\
& = n(n) \\
& = n^2 \\
& T(n) = O(n^2)
\end{aligned}$$

في كل تكرار نقوم بحذف العنصر في الموضع J الذي يتكرر عنده العنصر في الموضع I.
نبدأ من I=0 وننتقل إلى I=n-1.
في كل خطوة نبدأ من J=I+1 وننتقل إلى جملتنا الأخيرة.
إذا وجدنا أن العنصر في A[I] يساوي العنصر في A[J]، نحذف العنصر في A[J].
إذا لم نجد العنصر، ننتقل إلى العنصر التالي في J.
الوقت اللازم لتشغيل البرنامج هو مجموع الخطوات.
الخطوات لتكرار I هي (n-I).
الوقت الكلي هو مجموع هذه الخطوات من I=0 إلى I=n-1.
هذا هو مجموع الأعداد الطبيعية من 1 إلى n-1.
هذا يساوي $\frac{n(n-1)}{2} + n$ وهو $O(n^2)$.

```

pos = p -> next
p = A -> next
while (p -> next != Null)
{

```

```

  while (temp -> next != Null && temp -> element != p -> element)
  {
    temp = temp -> next
  }
  if (temp -> element == p -> element)
  {
    position = pre
    pre = find previous (A, temp -> element)
  }

```

Best case $O(n)$

8

Question #2(25%)

What is the worst case running time a function of n of the following function:

$$T(n) = \begin{cases} 2T(n/2) + 10 & n > 1 \\ 1 & n = 1 \end{cases}$$

(Hint: $X^{1-1} + X^{1-2} + \dots + 1 = (X^k - 1) / (X - 1)$)

$$\begin{aligned} T(n) &= 2T(n/2) + 10 \\ &= 2(2T(n/4) + 10) + 10 \\ &= 4(2T(n/8) + 10) + 20 + 10 \\ &= 8(2(T(n/16) + 10) + 40 + 20 + 10 \\ &\vdots \\ &= 2^k T_n + \sum_{i=1}^k 2^{i-1} 10 \end{aligned}$$

$T(1)$

توقف عند هنا

$n = 2^k \Rightarrow k = \log n$

$T(n) = 2^k T(1) + 10 \sum_{i=1}^k (2^{i-1}) \Rightarrow k$ عدد تكرار
 $= n + 10(2^k - 1)$



~~$T(n) = n + 10 \sum_{i=1}^{\log n} 2^{i-1}$~~

~~$T(n) = n + 10 \sum_{i=1}^{\log n} 2^{i-1}$~~

~~$T(n) \approx 2n$~~

~~$T(n) = O(n)$~~

~~$n + 10(2^{\log n} - 1)$~~
 ~~$= n + 10(2^n - 1)$~~

25

① ~~of a and b~~

Question #3(25%) ②

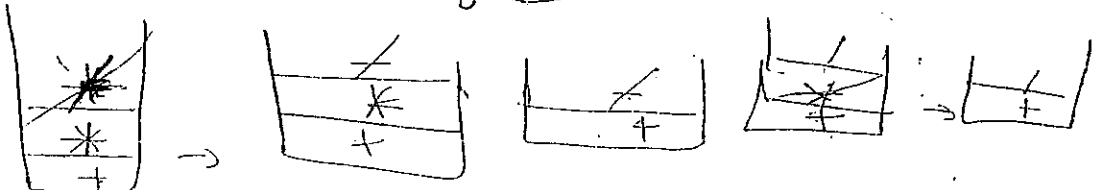
- a) Transform the following infix to postfix in details.
 b) Transform the following postfix to infix in details.

a) $a + a/2 * 5 - b * 3 / 2$

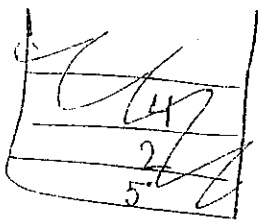
b) $5 2 4 / 3 * a / 2 / 7 * -$

$a / a / 2 / 5 * b * 3 * 2 / +$

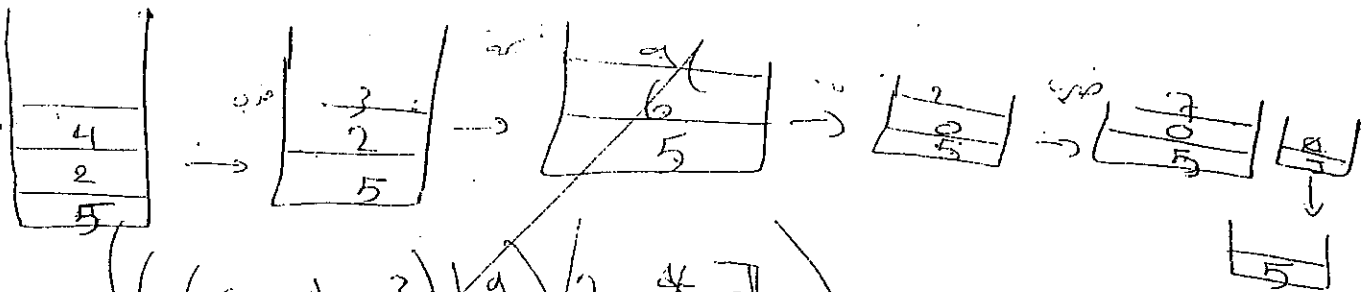
$a a 2 / 5 * + b 3 * 2 / -$



stack



$5 - ((2 / 4 * 3) / 9) / 2 * 7$



$5 - (((2 / 4) * 3) / 9) / 2 * 7$

50
5

الکواب 5

Question #4(25%)

Write a routine `addsame` to add two integers of the same sign represented by doubly linked lists.

```

typedef struct nod * next_ptr ;
typedef int element_type ;
struct nod

```

```

{
    node_ptr    pre ;
    node_ptr    next ;
    element_type element ;
} ;

```

```

typedef node_ptr position ;
typedef node_ptr header ;

```

```


element_type addsame ( header H )
{
    position temp ;
    element_type sum = 0 ;
    temp = H ;
    while ( temp->next != Null )
    {
        sum += temp->element ;
        temp = temp->next ;
    }
    return sum ;
}


```

```

void Insert ( position P, element_type e )

```

```

{
    position newnode ;
    newnode = (position) malloc ( sizeof(struct nod) ) ;
    newnode->next = Null ;
    newnode->element = e ;
    P->next = newnode ;
}

```


8/100

Computer Science Dept.
 Computer 232
 First Hour Exam

Instructor: Iyad Jaber

Date: 14/04/2003

Student Name: Haleem Aboud

No. 1011005

Question #1(15%):

What is the worst-case running time a function of n for the following code segment?

```

for (j = 0; j < n; j++)
  for (j = 0; j < i*i; j++)
    for (k = j; k < j*j; k++)
      cout << k;
    for (s = i; s < i*i; s++)
      cout << s;
  
```

$A = A + 1$

$n^3 [n^4 + n^2]$

$T(n) = (n) (n^2 - n) [(n^4 - n^2) + (n^2 - n)]$

$T(n) = n^3 - n^2 [n^4 - n^2]$

$T(n) = n^7 + n^4 - n^5 - n^6$

$T(n) = O(n^7)$

~~$1 + 2n [1 + 2n^2] [2n^4 + n^4 + 1 + 2n^3 + n^2]$~~

15

Question #2(30%):

a) Given the following definitions for a linked list of nodes:

```
typedef struct node * nodeptr;  
struct node
```

```
{  
    int element;  
    nodeptr next;
```

```
};
```

```
typedef nodeptr List, position;
```

Write a recursive function called `find(LIST L, int x)` which recursively looks for the integer `x` in linked list `L` and returns a pointer to `x` if it is found in `L`. Be sure to include any error checking necessary.

b) What is the worst case running time (Big_Oh notation) for the find function above?

```
position find (LIST L, int x) {
```

```
    position P;
```

```
    P = L->next;
```

```
    if (P && P->element == x)
```

```
        return P;
```

```
    else
```

```
        if (P && P->element != x)
```

```
            return find (P->next, x)
```

```
    else
```

```
        { cout << "the element " << x << " not found in n";
```

```
          exit (11);
```

```
        }
```

```
    }
```

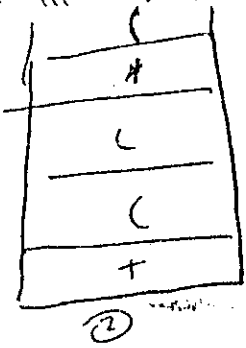
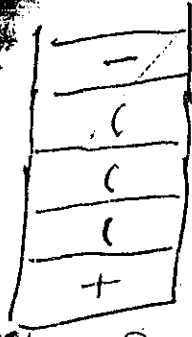
✓ 10/11

27

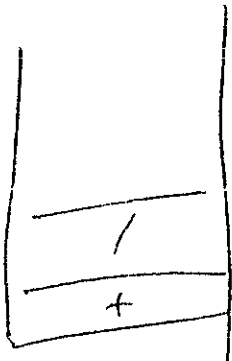
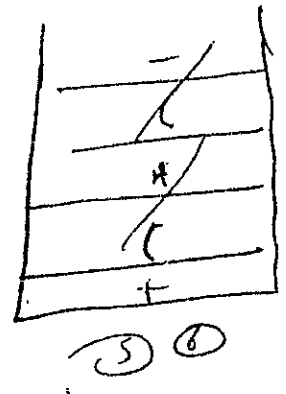
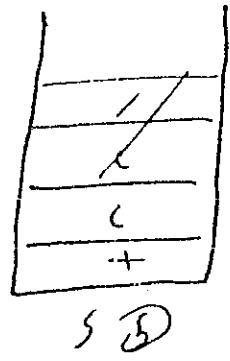
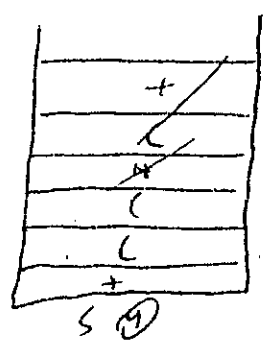
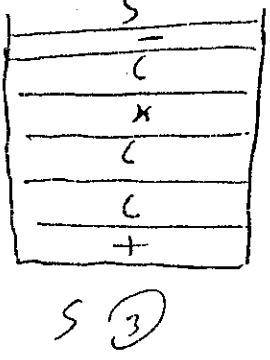
Question #3(25%):

Using a stack, transform the following infix expression to postfix. Show your work.

$$A + (((B - C) * (D - E + F) / G) * (H - J)) / K$$



~~ABC - DE - F + * G / H J - * K~~



~~ABC - DE - F + * G / H J - * K +~~

Question #4(30%):

Given the following definitions for a linked list of nodes:

```
typedef struct node { nodeptr;
```

```
struct node
```

```
{
```

```
int element;
```

```
nodeptr next;
```

```
};
```

```
typedef nodeptr List, position;
```

b) time

Write a function called SortList (List L), which takes a pointer to the linked list L, and then sort the elements inside the list in ascending order.

```
void SortList( List L)
```

```
{
```

```
position P; temp; // temp is stack.
```

```
P = L->next; temp = (position) malloc (sizeof(node));
```

```
getsmal(P) assert(temp);
```

```
temp->next = NULL; temp->next = NULL;
```

```
while (P) // n
```

```
{ push (temp, getsmal(P)); // n
```

```
cfree (P, getsmal(P));
```

```
}
```

```
L = temp;
```

```
}
```

```
int getsmal (position P)
```

```
{ while (P) int y = P->element;
```

```
while (P)
```

```
{ if (y > P->next->element)
```

```
swap (y, P->next->element);
```

```
else
```

```
P = P->next;
```

```
}
```

```
return y;
```

$$T(n) = (n) (n)$$

$$T(n) = O(n^2)$$

```
void swap (int tx, int ty)
```

```
{ int t = x;
```

```
x = y;
```

```
y = t;
```

```
}
```

14

19/60

Computer Science Dept.
Computer 232

Instructor: Iyad Jaber
Student Name: Datta Obaid

Date: 11/11/2003
No. 1011039

Question #1(20%):

Write a recursive function to add the first n terms of the series

float add (int n, float sum)

for (i=0; i<n; i++)

int fact (int n)

if (n == 0)
return sum = 1;

else

if (n > 0)
return

sum = ~~n fact n~~;

~~sum = n fact (n-1);~~

~~sum~~

~~sum = fact~~

return { ~~fact~~ }

~~sum = fact n~~

add (sum =) ;
}

add (int n)

if (n == 0)
return 0

else

return ~~2 * add (n-1) + 1~~;

$$1/2^n - 1$$

fact

if (n > 0)
return n * fact (n-1)

$$\left(\frac{1}{2^n - 1}\right)!$$

$$\frac{1}{2^n - 1} \text{ fact } \left(\frac{1}{2^n - 1} - \frac{1}{2^{n-1} - 1}\right)!$$

$$n = \frac{1}{2^n - 1}$$

$$\frac{1}{2^n - 1}$$

$$\left(\frac{1}{2^n - 1}\right)! + \left(\frac{1}{2^{n-1} - 1}\right)!$$

float add (int n, float sum)

for (i=0; i<n; i++)

add = fact n + fact n

$$2 * (2) = 5$$

$$2 * (1) = 3$$

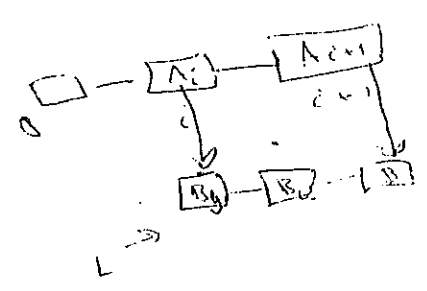
$$2 * (0) + 1 = 1$$

(5)

P → 1 3 4 6
 1 2 3 4 5 6
 1 2 3 4 5 6

Question #2(20%):

You are given a linked list, L, and another linked list, P, containing integers, sorted in ascending order. The operation `print_lots(L,P)` will print the elements in L that are in positions specified by P. For instance, if `P = 1,3,4,6`, the first, third, fourth, and sixth elements in L are printed. Write the routine `print_lots(L,P)`. You should use only the basic list operations. What is the running time of your routine? $O(n)$



```
void Print_lots (L, P)
```

```
    position p, temp;
```

```
    int
```

```
    int index n, i, j;  
    data * A, * B;  
    node * current;
```

```
    if (P == null)  
        cerr << "error";  
        exit (1);
```

```
    if (P->next == null)  
        return P;
```

```
    current = malloc (sizeof (struct node));
```

```
    A[i] = 0;  
    i = 0;
```

```
    current = current->next;  
    i++;
```

```
    while
```

```
    for (i = 0; i < n; i++)
```

```
        A[i] =
```

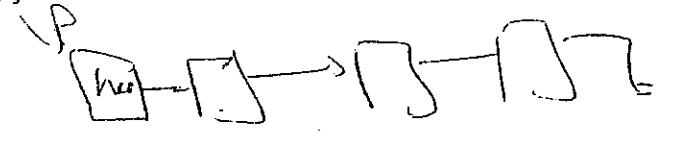
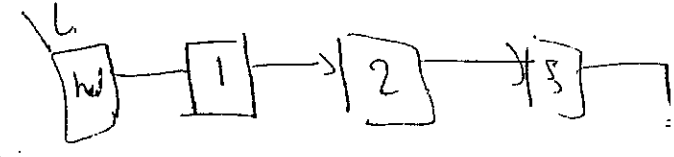
```
        j = A[i]
```

```
        j++;
```

```
    return B[i];
```

```
}
```

$T(n) = O(n \log n)$



```
void Print_lots (list L, list P)  
{  
    for (i = 0; i < n; i++)  
    if (P == 1)  
        cout << L->next->elem;
```

6

int noOfNodes (Tree T)

int count = 0;

if (T == null)

return 0;

if (T->left != null || T->right != null)

return 1

while (T->left != null) // for left side)

{ count++

T = T->left;

~~if (T->right != null)~~

count++

while (T->right != null) // for right side)

{ count++

T = T->right;

if (T->left != null)

count++

}

return count;

int noOf (Tree T)

if (T == 0)

return 0;

while (T->left != null || T->right != null)

{ T = T->left;

if (T->left != null || T->right != null)

count++

}

Question #3(20%):

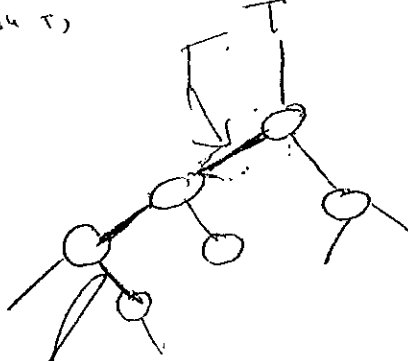
Write efficient functions that take only a pointer to a binary tree, T, and compute

- The number of nodes in T.
- The number of leaves in T.

What is the running time of your routines (in details)?

```

int nodeCounter ( struct T *
treePtr = T
if (T == null)
return 0;
if (T)
if (child == 0)
return 1;
else
if (T->left != null || T->right)
return count(T->left) + count(T->right);
else
return count(T->left) + count(T->right);
else
return count(T->left);
else
if (T->right)
return count(T->right);
}
    
```



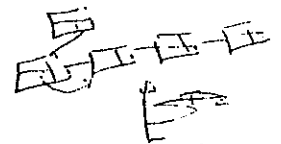
Count
1 2 3 4



(leaf)

• avoid
T->left = null
T->right = null

if T == null



na. ...
if ...
if ...
if ...
if ...

word number (Tree T)
x, y, z, a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z

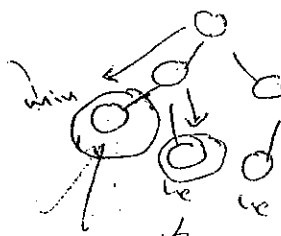
if (T == null)
{
 n = 0;
 l = 0;
}

else if (T->right != null && T->left != null)
 return count(T->right) + count(T->left) + 1;
else if (T->right != null && T->left == null)
 return count(T->right) + 1;
else if (T->right == null && T->left != null)
 return count(T->left) + 1;
else
 return 1;

$O(\log n)$ $O(n)$ Because it will be base on the while count them

```

int leavesCount ( struct T *
treePtr = T;
if (T == null)
return 0;
if (T->right == null && T->left == null)
return 1;
if (T->left != null)
return leavesCount(T->left);
if (T->right != null)
return leavesCount(T->right);
}
    
```



if (T->left != null)
 return leavesCount(T->left);
if (T->right != null)
 return leavesCount(T->right);
return 1;

T->right == null



$O(\log n)$

(8)

4/5
100

48
5
100
20
9.5
45
20

Computer Science Dept.
Comp. 232
First Hour Exam

Instructor: Iyad Jaber Fahad Alabdulmohsin 1020214 Date: 22/04/2004

Question #1(25%)

What is the worst case running time a function of n of the following function?

$$T(n) = \begin{cases} 2T(n/2) + 10 & n > 1 \\ d & n = 1 \end{cases} \quad \text{min}(x, L)$$

(Hint: $X^{n-1} + X^{n-2} + \dots + 1 = (X^n - 1) / (X - 1)$)

$$\frac{x^n - 1}{x - 1}$$

$$T\left(\frac{n}{2}\right) = \begin{cases} 2T\left(\frac{n}{4}\right) + 10 & n > 1 \\ d & n = 1 \end{cases}$$

$$T(n) = \cancel{2T\left(\frac{n}{2}\right)} + 10 = 2\left(2T\left(\frac{n}{4}\right) + 10\right) + 10$$

$$= 4T\left(\frac{n}{4}\right) + 20 + 10$$

$$= 4T\left(\frac{n}{4}\right) + 30$$

$$= 2^2 T\left(\frac{n}{2^2}\right) + 2 \cdot 15$$

$$= 2^i T\left(\frac{n}{2^i}\right) + \dots$$

let $2^i = n \Rightarrow \log_2 n = i$

$$= n T(1) + 2 \log_2 n$$

$$= n(d) + 2 \log_2 n$$

$$= nd + 2 \log_2 n$$

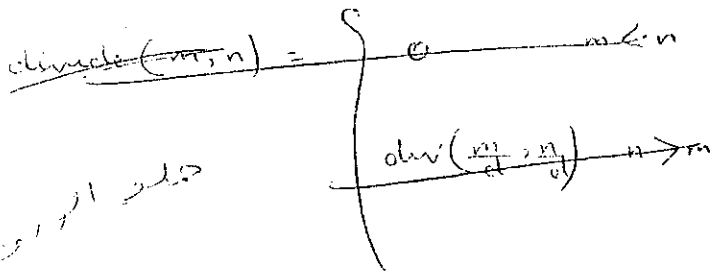
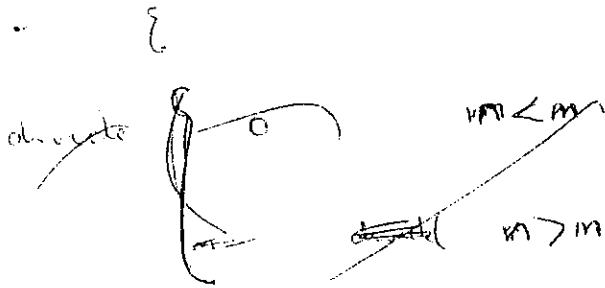
$$O(n)$$

(8)

Question #2(25%)

Write a recursive function called `divide(m, n)` which takes two positive integers, `m` and `n`, and returns the `n` DIV `m` without using `/` operation.

~~void divide (int m, int n).~~



```

int divide (int m, int n)
{
    if ( n < m )
        return 0;
    else
        if ( n < m )
            if ( n == m )
                return 1;
            else
                if ( n > m )
                    return divide (m, n)
                    return divide (m, n - m);
    }
}

```

Handwritten notes and calculations illustrating the recursive process:

- Examples of division: $10/5 = 2$, $20/5 = 4$, $30/5 = 6$, $28/7 = 4$, $28/2 = 14$.
- Recursive calls: $divide(28, 7) = 1 + divide(28, 21)$, $divide(28, 21) = 1 + divide(28, 14)$, $divide(28, 14) = 1 + divide(28, 7)$.
- Diagrammatic representation of the recursive stack with arrows indicating return values.
- Arithmetic showing how multiplication can be used to verify results: $10 = 2 \times 5$, $20 = 4 \times 5$, $28 = 4 \times 7$.
- Additional calculations: $10/3 = 3$, $10/2 = 5$, $10/1 = 10$.

Question #3(25%)

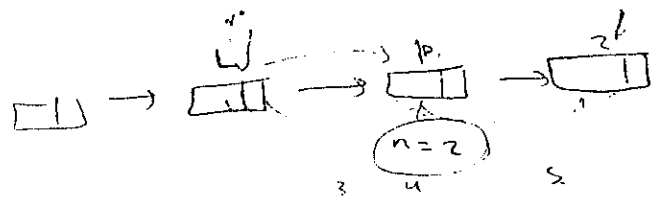
Write a function that receives a circular linked list L and an integer value n. The function should delete the nth element from the list starting from the L and then continues to delete the nth element circularly until the number of nodes becomes less than n.

```


void delete (list L, int n)
{
    struct node * ptr;
    struct node
    {
        elementtype element;
        ptr next;
    };
    typed ptr list;
    typed ptr position;

    void delete (list L, int n)
    {
        if (L == null)
        {
            if (L->next != null)
            {
                L->next = L->next->next;
            }
            if (L->next == L)
            {
                // ...
            }
        }
    }
}


```



```

void delete (list L, int n)
{
    position p;
    p = L;
    int s, // number of nodes
    IF (s > n)
    {
        p = p + n;
    }
    free (p->next);
    s = s - n;
    else
    IF (n > s)
    cout << "no node";
}

```

8

Question #4(25%)

Show how to implement a queue of integer in C++ by using linked list implementation, and then write the routines **remove**, **insert**, and **empty** for such an implementation.

```
typedef struct node *ptr,
struct node
```

```
{ element type element;
  ptr next;
};
```

```
typedef ptr Queue,
typedef ptr position;
```

```
void remove (Queue q) ...
```

```
{ position p;
```

```
  p = q ...;
```

```
  if (p (p->next != null))
```

```
    p = p->next;
```

```
  else free(p); }
```

```
temp = q->next;
```

```
temp->next = null;
```

```
void insert (Queue q, element type x)
```

```
{ position p;
```

```
  p = q;
```

```
  if (p->next != null)
```

```
    p = p->next;
```

```
  else
```

```
    position temp;
```

```
    temp = (position) malloc (sizeof (struct node));
```

```
    Assign (temp, null);
```

```
temp->next = null;
```

```
temp->element = x;
```

```
temp->next = p->next;
```

```
}
```

```
void node.empty (Queue q)
```

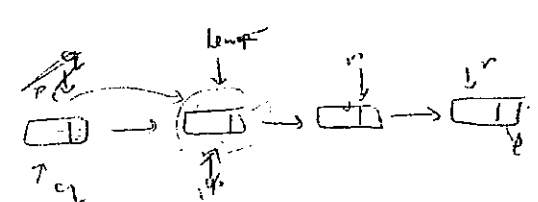
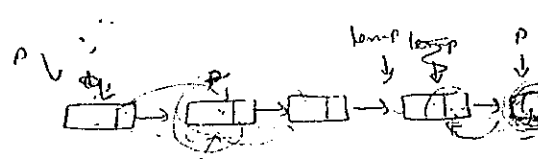
```
{ position p, temp;
```

```
p = q->next; if (p->next == null)
```

```
if (p->next != null) else
```

```
cont << "Queue is empty\n";
```

```
if (p->next != null)
```



17

43/105

Instructor: Iyad Jaber
Student Name: ~~XXXXXXXXXX~~

Date: 17/04/2007
No. ~~XXXXXX~~

Question #1(25%):

What is the worst case running time a function of n of the following function?

```
void confuse( int a[], int left, int right)
{
    if ( left < right)
    {
        ...
        ...
        ...
    }
    ...
    Confuse( a, left, (left + right)/2 );
    Confuse( a, (left + right)/2, right );
}
```

$T(n) = \begin{cases} * & n = 1 \\ T(\frac{n}{2}) + C(n) & n > 1 \end{cases}$

* $T(n) = T(\frac{n}{2}) + n$
 $T(\frac{n}{2}) = T(\frac{n}{2^2}) + n \implies$
 ~~$T(n) = 2(T(\frac{n}{2}) + n) + n$~~
 ~~$T(n) = 2^2 T(\frac{n}{2^2}) + 2n + n$~~
 ~~$T(\frac{n}{4}) = T(\frac{n}{2}) + n$~~
 $T(\frac{n}{4}) = 2(T(\frac{n}{2^3}) + n)$
 ~~$T(n) = T(\frac{n}{2^3}) + 3n$~~
 ~~$T(n) = 2^2(2(T(\frac{n}{2^3}) + n) + 3n$~~
 $= 2^3 T(\frac{n}{2^3}) + 7n$

$T(n) = (T(\frac{n}{2^2}) + n) + n$
 $T(\frac{n}{4}) = T(\frac{n}{2^3}) + n$
 $T(n) = T(\frac{n}{2^3}) + n + 2n$
 $T(n) = T(\frac{n}{2^k}) + kn$
 let $n = 2^k \implies k = \log_2 n$
 $T(n) = T(1) + n \log_2 n$
 $T(n) = 1 + n \log_2 n$
 $T(n) = O(n \log_2 n)$

```
int check(char str[], int left, int right)
```

```
{ if (left > right)
```

```
    if (str[left] != str[right])
```

```
        return 0;
```

```
    else
```

```
        return (check(str, left+1, right-1));
```

```
    return 1;
```

```
}
```

Question #2(25%):

Write a recursive function to determine whether or not a string consisting of all uppercase letters is a palindrome. Note that 'FABBAF' and 'CEDEC' are palindromes, whereas 'GAEG' is not.

```
#include <string.h>
```

```
int palindrome (char string, int A)
{
    int C = strlen(string);
    if (C % 2 == 0)
        return 0;
    else
        return while (string != "0")
        return (for (int i = 0; i < C; i++)
        if (string[i] == string[C-i-1])
            return 1; }
}
```

int palindrome

RECURSIVE

```
#include <string.h>
```

```
int palindrome (char string)
{
    if (strlen(string) % 2 == 0)
        return 0;
    else
        string = strcmp (string, string/2)
        return palindrome (string);
    else return 1;
}
```

8

ptr reverse(ptr L)

{ ptr A, P, K;

A = L;

if(L)

 P → L → next;

 A → next = Null;

 while(P)

 { K = P → next

 P → next = A;

 A = P;

 P = K;

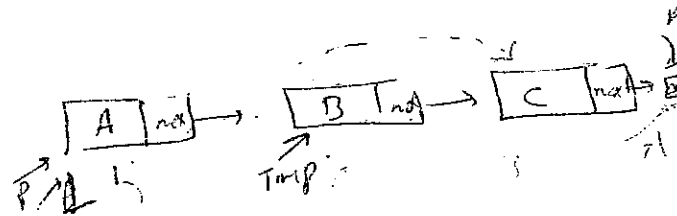
 } return A; }

Question #3(25%):

Write a procedure to reverse the pointers in a linked list. For example,
A → B → C → D would become A ← B ← C ← D. (don't use extra linked list)

```
type def struct Node {  
  element: type element;  
  position: Next };  
type def ptr Node list;  
type def ptr Node position;
```

```
List reverse(list L)  
{ position p, position tmp;  
  p = L; next  
  for ( ; p != Null; p = p → next )  
  while ( p != Null )  
  tmp = p → next;  
  p → next = tmp → next;  
  tmp → next = p → next → next;  
  if ( tmp → next == Null )  
  tmp → element = p → element  
  L = L → next;  
  return L;  
}
```



(J)

```
int height(BST T)
```

```
{ if (T == null)
```

```
    return -1;
```

```
    else
```

```
    return (max(height(T->left), height(T->right)) + 1);
```

```
}
```

```
int leaves(BST T)
```

```
{ if (T == null)
```

```
    return 0;
```

```
    else
```

```
    if (T->left == null & (T->Right == null))
```

```
        return 1;
```

```
    else
```

```
    return (leaves(T->left) + leaves(T->Right));
```

```
}
```

Question #4(25%):

Write efficient functions that take only a pointer to a binary tree, T, and compute

- The height of the tree.
- The number of leaves in T.

What is the running time of your routines (in details)?

```

type def struct tree {
    = tree *ptr;
    = ptr p;
}
struct tree {
    int element type element;
    p left;
    p right;
    int height;
}
    
```

```

int height (Tree T)
    int counter
    {
        if (T == Null)
            return -1;
        else
            if (T->right == null && T->left == null)
                return 0;
            else
                return max(T->left, T->right)
    }
    
```

```

int max(T->left, T->right)
    {
        if (T->left == null)
            height++;
            return max(T->left, T->right);
        else if (T->right != null)
            height++;
            return max(T->left, T->right)
        else return right;
    }
    
```

```

int leaves (tree T)
    int counter;
    if (T == Null)
        cout << "no leaves";
    while (T->right && T->left)
        return counter++;
    }
    
```

$T(n) = O(n)$

all nodes 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100

$T(n) = O(\log n)$

لانه عدد نودها فقط نصف ميشود
 در هر مرحله نصف ميشود
 Binary
 تا به جايي كه فقط يك نود باقى بماند

